# Quantitative Methods

## Study Session 3 Quantitative Methods

### Reading 6 Fintech in Investment Mgmt

#### Data Science

Data processing: capture/ curation (data quality and accuracy assurance)/ storage/ search/ transfer (from data source/ storage to analytical tool)

Data visualization: heat map, interactive 3-D, tag cloud, network graphs, tree diagrams

#### Selected Applications of Fintech to IM

Text analytics and NLP: analyze annual report, transcripts, policy statements, voices etc.

Robo-Advisory Services: fully automated/ advisor-assisted

Risk Analysis: stress testing and risk assessment

Algorithmic Trading: HFT

#### DLT

Not fully secure, breaches in privacy and data protection are possible.

DLT: a type of database that may be shared among entities in a network.

Cryptography: an algorithmic process to encrypt data, making data unusable if received by unauthorized parties.

Smart contracts: self-execute programs

Blockchain: a type of digital ledger in which info is recorded sequentially within blocks, that are then linked or “chained” together, and secured using cryptographic methods.

Permissioned and Permission-less Networks

DLTG Applications:

1. Cryptocurrencies: ICO
2. Tokenization: representing ownership rights to physical assets on a blockchain or DLT. A single, digital record of ownership with which to verify ownership title and authenticity, including all historical activity.
3. Post-trade clearing and settlement: confirm, clear and settle transactions among counterparties and intermediaries.
4. Compliance: shared information, communications, transparency within and between firms, exchanges, custodians and regulators. Security and privacy in closed or permissioned networks.

### Reading 7 Correlation and Regression

Sample covariance：协方差 | Sample correlation coefficient：相关系数

Limits to correlation analysis

Formulate a hypothesis test – put correlation coefficient to zero and reject at a give level of significance to prove they are related

Dependent and independent variables in a linear regression

Assumptions under linear regression and explain regression coefficient

Calc and interpret standard error estimate | coefficient of determination | a confidence interval for a regression coefficient

A null and alternative hypothesis for a regression coefficient, proper test stats, reject null hypothesis at a given significance level

Calc predicated value for the dependent variable, given an estimated regression model and value of independent variable.

A confidence interval for the dependent variable predicated value.

ANOVA (analysis of variance) in regression analysis, interpret ANOVA results, calc and interpret F-stats

Limits of regression analysis

#### Correlation analysis

Measure how two variables vary in relation to each other.

##### Scatter plots

##### Correlation analysis

Correlation coefficient vary between 1 and -1. 1和-1代表完全在一条直线上而没有散发，0代表完全不在一条直线。

##### Calc and interpret correlation coefficient

计算相关系数要用到协方差和样本方差 – 两个变量分别和他们样本均值差的乘积的平均值（除以n-1而不是n）。

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n: sample size

C:\Users\Li\AppData\Local\Temp\ksohtml16636\wps2.jpg: ith observation on variable X

C:\Users\Li\AppData\Local\Temp\ksohtml16636\wps3.jpg: mean of the variable X observations

C:\Users\Li\AppData\Local\Temp\ksohtml16636\wps4.jpg: ith observation on variable Y

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**协方差表示的是两个变量的总体[误差](https://baike.baidu.com/item/%E8%AF%AF%E5%B7%AE/738024)**，这与只表示一个变量误差的[方差](https://baike.baidu.com/item/%E6%96%B9%E5%B7%AE/3108412)不同。 如果两个[变量](https://baike.baidu.com/item/%E5%8F%98%E9%87%8F/5271)的变化趋势一致，也就是说如果其中一个大于自身的期望值，另外一个也大于自身的期望值，那么两个变量之间的协方差就是正值。 如果两个变量的变化趋势相反，即其中一个大于自身的期望值，另外一个却小于自身的期望值，那么两个变量之间的协方差就是负值。

A measure of the strength of the linear relationship (correlation) between two variables.

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##### Limits of correlation analysis

Not reliable in case of nonlinear relation

Impact of outlier

Does not imply causation（因果论）

Spurious correlation caused by:

1. A particular dataset
2. A calculation mixed each of two variables with a third
3. Arising not from a direct relation but from their relation to a third variable

##### Uses of correlation analysis

Evaluating forecast

Style analysis

Correlations are always symmetrical

##### Testing correlation coefficient significance

用t分布做双尾检验，如果显著性水平上落在区间外就拒绝。显著性水平α要除以2得到t表查表概率p。

检验估计的相关系数的显著性。

Test whether the correlation between the populations of two variables is equal to zero. (If it is zero, it means there is no correlation, otherwise there is.) Use the sample correlation to compute the test statistic.

Two tailed test:双尾检验

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假设两个样本集合都是正态分布，使用t检验来决定是否拒绝空假设（即支持两个样本之间有关系）。T的值用样本相关系数r来计算。T检验用在样本数小于30，总体方差未知的情况。如果样本数大于30，且方差已知，则使用Z检验。

Assuming the two populations are normally distributed, we can use a *t-*test to determine whether the null hypothesis should be rejected. The test statistic is computed using the sample correlation, *r*, with **n-2 degrees of freedom (*df*).**

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Compare the test statistic with the critical *t*-value for the appropriate degrees of freedom and level of significance.  The decision rule can be stated as:

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Z检验用于大样本（大于30）平均值差异性检验

Z=\frac{\bar{X}-\mu_0}{\frac{S}{\sqrt{n}}}

**T检验用于小样本（小于30），总体方差未知的正态分布**

F检验用于两样本检验

#### Linear Regression

Linear regression assumes a linear relationship between the dependent and independent variables.

线性回归主要使用两类数据：cross sectional 和time series

Linear regression aka linear least squares, computes a line that best fits the observations. It chooses values for the intercept b0 and slope b1, that minimize the sum of the squared vertical distances between observations and regression lines.

=*i*th observation of the dependent variable, Y

=*i*th observation of the independent variable, X

=regression intercept term（回归截距）

=residual for the *i*th observation (also refer to as the disturbance term – 扰动项,or error term – 错误项)

回归过程就是从一个散点图中估计出一条直线的等式，能最好解释从观察到Y值对应到观察到的X值。

线性等式，或者叫最佳匹配线，或者叫回归线，等式如下：

=给定，的估计值

=估计得截距

=估计的斜率系数

帽子符号^代表预计的值

回归线是估计值和真实值之间差的平方的和最小的线。估计值和真实Y值（垂直距离）的差的平方和，也叫平方误差和（sum of squared errors – SSE ）。回归线就是让SSE最小的线。这也解释了为什么简单**线性回归经常被叫做最小二乘（ordinary least squares - OLS）回归**，而估计回归公式得到的值也叫作最小二乘估计。

**斜率系数等于，截距用平均值加上斜率来求解。**

##### Linear regression model assumptions

1. Relationship between dependent variable and independent variable is linear: if the dependent variable is nonlinear, linear regression can be used as long as the regression is linear in the parameters.
2. Independent variable is not random
3. Expected value of the error term is 0: ;
4. The variance of the error term is the same for all observations: . homoskedasticity
5. Error term ε is uncorrelated across observations. for all
6. Error term ε is normally distributed

##### Standard error of estimate

How well a given linear regression model captures the relationship between the dependent and independent variables.

SSE is sum of standard error

计算要考的！

##### The Coefficient of Determination

Two methods:

1. Simpler: only has 1 independent variable. Simply use square of the correlation coefficient to show the determination percentage;
2. General: multiple independent variables.

衡量因变量的总体变化程度，真实Y值和平均值之间的差的平方和。和方差不尽相同，**方差variance=SST/(n-1)；**

预测值和平均值之间的差的平方和, 衡量由独立变量所揭示的**因变量的变化程度**。

真实值和预测值之间的差的平方和。**因变量中未被解释的部分**。

##### Hypothesis testing

The most common way to test a hypothesis using a regression model is with a t-test of significance.

t检验可以被用来检验真是斜率系数是否等于某个假设值。 给定的点估计，n-2自由度下的检验统计量是：

Reject if

拒绝假设代表着斜率系数与假设值不一样。

有时候不会直接报是否拒绝关于回归参数的特定假设，他们会报告p-value。这个p-value是空假设能被拒绝的最小显著性水平。

If p-value is 0.005, we can reject the hypothesis at the true parameter is equal to 0 at 0.5 percent significance level (99.5 percent confidence).

Regression analysis: Examine the ability of one or more variables (independent variables) to explain or predict dependent variable.